4.1 HW: Simplifying Rational Expressions

1. The length of a rectangular prism is 9 more than the width. The volume is $w^3 + 8w^2 - 9w$. What is the *simplified* expression for the height of the prism?

2. Write a rational expression that has 4 and -3 as excluded values.

3. A square has a side length of x + 4. A rectangle with a height of 2x + 8 has the same area as the square. Write an expression for the length of the rectangle.

Simplify and state the excluded values.

4.
$$\frac{k+3}{k^2+8k+15}$$

5.
$$\frac{x^2 + 2x + 1}{x + 1}$$

6.
$$\frac{n-2}{n^2 - 7n + 10}$$

7.
$$\frac{20n^2 + 12n}{12n}$$

8.
$$\frac{6b^2 - 14b}{4b^2 + 6b}$$

9.
$$\frac{b^2 + b - 12}{b^2 - 9b + 18}$$

10.
$$\frac{9m - 27}{m^2 - 11m + 24}$$

11.
$$\frac{n^2 + 6n + 9}{n^2 + 9n + 18}$$

12.
$$\frac{21p^2 + 35p}{21p^2 - 28p}$$

13.
$$\frac{r^2 - 6r + 9}{r^2 - 10r + 21}$$

14.
$$\frac{n^2 - 36}{n^2 - n - 42}$$

15.
$$\frac{k^2 + 14k + 48}{k^2 - 4k - 60}$$

16.
$$\frac{18x^3 + 30x^2 + 12x}{42x^3 + 90x^2 + 12x}$$

$$17. \ \frac{2x+16}{5x^3+39x^2-8x}$$

Perform the following operations.

18.
$$\frac{1}{3} \cdot \frac{2}{5}$$

19.
$$\frac{11}{5} \div 2$$

20.
$$\frac{3}{4} + \frac{2}{3}$$

21.
$$\frac{8}{12} - \frac{3}{8}$$